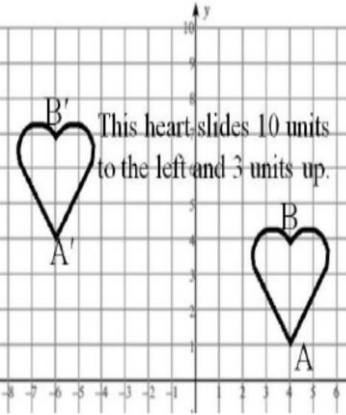


Math 8 Georgia Milestones Review Sheet

Unit 1: Transformations, Congruence, and Similarity

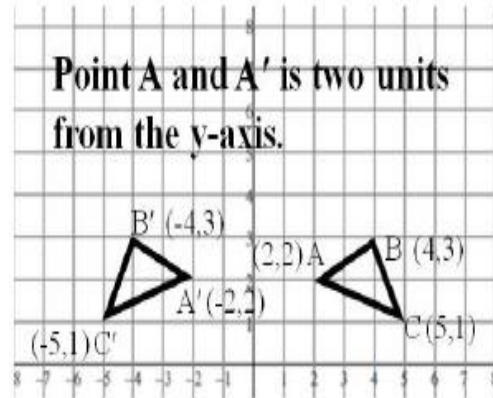
Transformations...

Translation - "slides" each point of a figure the same distance in the same direction without changing its size or shape and without turning it or flipping it.



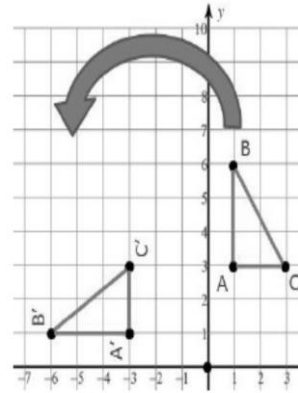
SLIDE

Reflection - "flips" a figure over a mirror or reflection line; An object and its reflection have the same shape and size, but the figures face in opposite directions.



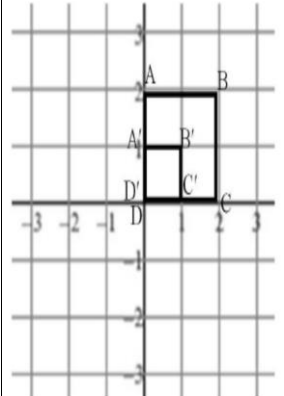
FLIP

Rotation - turns a figure about a fixed point at a given angle and a given direction; An object and its rotation are the same shape and size, but the figures may be turned in different directions.



TURN

Dilation - proportionally changes the size of an object (by shrinking or stretching), but not the shape.



ENLARGE/REDUCE

Translations Rules:

A positive integer describes a translation right or up on a coordinate plane.

A negative integer describes a translation left or down on a coordinate plane.

A movement left or right is on the x-axis.

A movement up or down is on the y-axis.

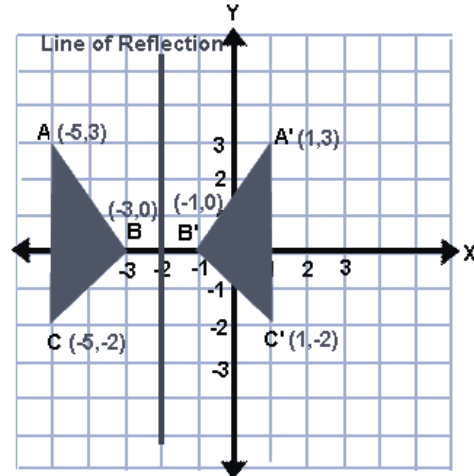
Reflection Rules:

Reflect a figure over the x-axis- when reflecting over the x-axis, change the y-coordinates to their opposites. **(x, -y)**

Reflect a figure over the y-axis- when reflecting over the y-axis, change the x-coordinates to their opposites. **(-x, y)**

Reflection over any line

Each point of a reflected image is the same distance from the line of reflection as the corresponding point of the original figure.



Notice how each point of the original figure and its image are the same distance away from the line of reflection (which can be easily counted in this diagram since the line of reflection is vertical).

Rotation Rules:

90 degree clockwise rotation around the origin (0,0), use: **(y, -x)**

180 degree rotation around the origin (0,0), use: **(-x, -y)**

270 degree clockwise rotation around the origin (0,0), use: **(-y, x)**

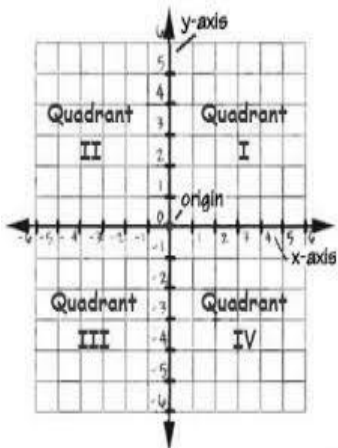
Dilation Rules:

To dilate a figure, always **MULTIPLY** the coordinates of each of its points by the percent of dilation.

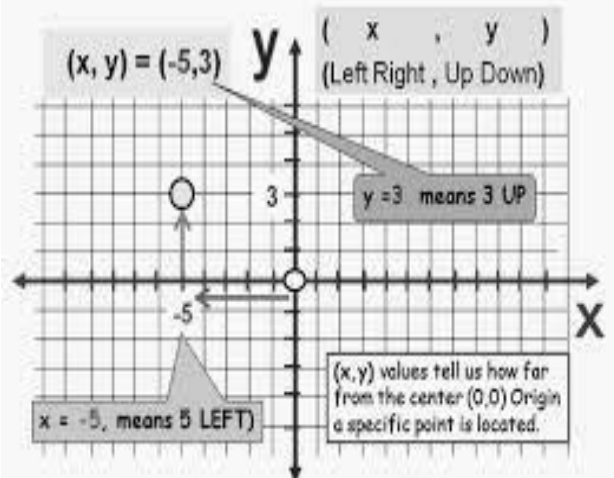
First change the percent to a decimal (move the decimal point **TWO** places to the **LEFT**).

Next, multiply each of the coordinates by that number.

Coordinate Plane:



Coordinates - (x,y) Points



Angles...			
Relationships		Measurements	
	Alternate Interior $\angle 3$ & $\angle 6$ Alternate Exterior $\angle 2$ & $\angle 8$ Consecutive Interior $\angle 4$ & $\angle 6$ Corresponding $\angle 1$ & $\angle 5$ Vertical $\angle 2$ & $\angle 3$ Adjacent $\angle 7$ & $\angle 8$		$m\angle 1 = 55^\circ$ $m\angle 2 = 125^\circ$ $m\angle 3 = 125^\circ$ $m\angle 4 = 55^\circ$ $m\angle 5 = 55^\circ$ $m\angle 6 = 125^\circ$ $m\angle 7 = 55^\circ$
Supplementary angles = 180° Complementary angles = 90° Linear Pair: Two angles that are adjacent (share a leg) and supplementary (add up to 180°)	Corresponding angles = on the same side of the transversal (one angle is an interior and one is an exterior) Vertical angles are opposite of each other and have the same measurement; are congruent (\cong)	Alternate interior angles are opposite each other and inside two parallel lines which are cut by a transversal; have the same measurement; are congruent (\cong)	Alternate exterior angles are opposite each other and outside two parallel lines which are cut by a transversal; have the same measurement; are congruent (\cong)

Unit 2: Exponents and Equations

Estimating Radicals:	Scientific Notation:	Multiplying:	Dividing:
1) Draw a number line 2) Find the closest perfect squares – one smaller and one larger 3) Eliminate answer choices	$3,420,000 = 3.42 \times 10^6$ $.00000000986 = 9.86 \times 10^9$ 1. Place decimal behind first non 0 number 2. Multiply by 10 3. Count spaces new to old (exponent) Left = negative and right = positive	$(2.3 \times 10^5) (1.4 \times 10^2)$ 1) $2.3 \times 1.4 = 3.22$ 2) $10^5 \times 10^2 = 10^7$ 3) 3.22×10^7	$(6 \times 10^8) \div (2 \times 10^2)$ 1) $6 \div 2 = 3$ 2) $10^8 \div 10^2 = 10^6$ 3) 3×10^6

Square Roots

Know perfect square roots to 25.	Know perfect cube roots to 10.	Know:	Know:
$1^2 = 1$ $2^2 = 4$ $3^2 = 9$ $4^2 = 16$ $5^2 = 25$ $6^2 = 36$ $7^2 = 49$ $8^2 = 64$ $9^2 = 81$ $10^2 = 100$ $11^2 = 121$ $12^2 = 144$ $13^2 = 169$ $14^2 = 196$ $15^2 = 225$ $16^2 = 256$ $17^2 = 289$ $18^2 = 324$ $19^2 = 361$ $20^2 = 400$ $21^2 = 441$ $22^2 = 484$ $23^2 = 529$ $24^2 = 576$ $25^2 = 625$	$1^3 = 1$ $\sqrt[3]{1} = 1$ $2^3 = 8$ $\sqrt[3]{8} = 2$ $3^3 = 27$ $\sqrt[3]{27} = 3$ $4^3 = 64$ $\sqrt[3]{64} = 4$ $5^3 = 125$ $\sqrt[3]{125} = 5$ $6^3 = 216$ $\sqrt[3]{216} = 6$ $7^3 = 343$ $\sqrt[3]{343} = 7$ $8^3 = 512$ $\sqrt[3]{512} = 8$ $9^3 = 729$ $\sqrt[3]{729} = 9$ $10^3 = 1000$ $\sqrt[3]{1000} = 10$	$\sqrt{0} = 0$ $\sqrt{\quad} = \text{radical}$	$1^0 = 1$ $55^0 = 1$ $100^0 = 1$ Anything to the raised to the zero power is one.

Rational and Irrational Numbers

Rational Numbers	Irrational Numbers
Is a number that can be expressed as a fraction or ratio. The numerator and the denominator of the fraction are both integers. When the fraction is divided out, it becomes a terminating or repeating decimal. Examples: $\frac{2}{3}$ 0.25 $\frac{1}{2}$ 0.666	Cannot be expressed as a fraction. Irrational numbers cannot be represented as terminating or repeating decimals. Irrational numbers are non-terminating, non-repeating decimals. Example: $\pi = 3.141592654.....$ $\sqrt{2} = 1.414213562.....$ 0.1211211121112

Exponent Rules – must have the same base!! Keep the base!!

<p>Multiplying: add exponents $4^2 \times 4^6 = 4^8$</p>	<p>Dividing: subtract exponents $\frac{6^8}{6^5} = 6^3$</p>	<p>Power to a Power: multiply exponents $(3^5)^2 = 3^{10}$</p>	<p>Negatives: flip to become positive $2^{-6} = \frac{1}{2^6}$ <i>**Does not apply to scientific notation</i></p>
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Properties

<p>Commutative Property of Addition Changing the <i>order</i> of the addends does not change the sum.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $a + b = b + a$ $5 + 9 = 9 + 5$ $14 = 14$ </div> <p style="text-align: right; border: 1px dashed black; border-radius: 50%; padding: 2px; display: inline-block;">Think "order"</p>	<p>Associative Property of Addition Changing the <i>grouping</i> of the addends does not change the sum.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $(a + b) + c = a + (b + c)$ $(1 + 4) + 7 = 1 + (4 + 7)$ $5 + 7 = 1 + 11$ $12 = 12$ </div> <p style="text-align: right; border: 1px dashed black; border-radius: 50%; padding: 2px; display: inline-block;">Think "grouping"</p>	<p>Identity Property of Addition The sum of zero and a number is that number.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $a + 0 = a$ $0 + a = a$ $89 + 0 = 89$ $0 + 89 = 89$ </div> <p style="text-align: right; border: 1px dashed black; border-radius: 50%; padding: 2px; display: inline-block;">Think "same"</p>	<p>Zero Property of Multiplication The product of zero and a number is zero.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $0 \times a = 0$ $a \times 0 = 0$ $0 \times 33 = 0$ $33 \times 0 = 0$ </div> <p style="text-align: right; border: 1px dashed black; border-radius: 50%; padding: 2px; display: inline-block;">Think "0 product"</p>
<p>Commutative Property of Multiplication Changing the <i>order</i> of the factors does not change the product.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $a \times b = b \times a$ $3 \times 8 = 8 \times 3$ $24 = 24$ </div>	<p>Associative Property of Multiplication Changing the <i>grouping</i> of the factors does not change the product.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $(a \times b) \times c = a \times (b \times c)$ $(6 \times 5) \times 2 = 6 \times (5 \times 2)$ $30 \times 2 = 6 \times 10$ $60 = 60$ </div>	<p>Identity Property of Multiplication The product of one and a number is that number.</p> <div style="border: 1px solid black; padding: 5px; margin: 5px;"> $1 \times a = a$ $a \times 1 = a$ $1 \times 8 = 8$ $8 \times 1 = 8$ </div>	

<p>Order of Operations</p> <p>Step 1: Complete the operation inside of the parentheses first.</p> <p>Step 2: Complete any exponents.</p> <p>Step 3: Multiply & Divide IN ORDER from LEFT to RIGHT.</p> <p>Step 4: Add & Subtract IN ORDER from LEFT to RIGHT.</p> <p>Example: $48 \div 8 + 6(4 + 2) - 15$</p> <p>Step 1: $6(4 + 2) = 6(6) = 36$ Next Line: $48 \div 8 + 36 - 15$ Step 2: $48 \div 8 = 6$ Next Line: $6 + 36 - 15$ Step 3: $6 + 36 = 42$ Next Line: $42 - 15 = 27$</p>	<p>Inverse Property of Addition Adding the opposite (additive inverse) of a number to the number will give you a sum zero.</p> <p>Example: $a + (-a) = 0$ $(-a) + a = 0$</p> <p>$14 + (-14) = 0$ $(-14) + 14 = 0$</p>	<p>Inverse Property of Multiplication If you multiply a number by its reciprocal (multiplicative inverse) the product is 1.</p> <p>Example: $a \times 1/a = 1$ $1/a \times a = 1$</p> <p>$9 \times 1/9 = 1$ $1/9 \times 9 = 1$</p>	<p>Distributive Property Multiply a sum by multiplying each addend separately and then add the products.</p> <p>$5(x + 2) = 5(x) + 5(2) = 5x + 10$</p> <p>**Can NOT combine unlike terms</p>
		<p>Like terms Terms whose variables (and their <u>exponents</u> such as the 2 in x^2) are the same. In other words, terms that are "like" each other. Example: $7x \quad x \quad -2x$ Are all like terms because the variables are all x</p>	<p>Unlike Terms Example: $-3xy \quad -3y \quad 12y^2$ these are all unlike terms (xy, y and y^2 are all different)</p>

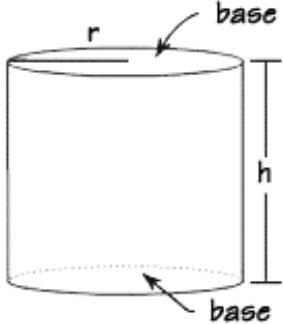
<p>Expressions</p> <p>An expression is a mathematical "phrase" that stands for a single number.</p> <p>An equation consists of two expressions connected by an equals sign.</p> <p>It can only be true or false.</p> <p>Example: a number less than five $5 - x$ five less than a number $x - 5$</p>	<p>Equations</p> <p>An equation is a mathematical "sentence" that says that two things are equal.</p> <p>An expression is never true or false, but just has a numerical value.</p> <p>Example: Ten is five less than a number. $10 = x - 5$</p> <p>A number is less than five. $x < 5$</p>	<p align="center">Linear Equations</p> <p>Solving a Linear Equation : Get the variable you are solving for alone on one side and everything else on the other side using INVERSE operations.</p> <p>Example:</p> <table style="width: 100%; border-collapse: collapse;"> <tr> <td style="width: 33%;">$x - 5 = 2$</td> <td style="width: 33%;">$5x = 7$</td> <td style="width: 33%;">$\frac{x}{2} = 5$</td> </tr> <tr> <td>$x - 5 + 5 = 2 + 5$</td> <td>$\underline{5x} = \underline{7}$</td> <td>$\frac{(2)}{2} \frac{x}{2} = (2)5$</td> </tr> <tr> <td>$x = 7$</td> <td>$5 \quad 5$</td> <td>$x = 10$</td> </tr> <tr> <td>$y + 4 = -7$</td> <td>$\underline{x} = \underline{\frac{7}{5}}$</td> <td></td> </tr> <tr> <td>$y + 4 - 4 = -7 - 4$</td> <td></td> <td></td> </tr> <tr> <td>$y = -11$</td> <td></td> <td></td> </tr> </table>	$x - 5 = 2$	$5x = 7$	$\frac{x}{2} = 5$	$x - 5 + 5 = 2 + 5$	$\underline{5x} = \underline{7}$	$\frac{(2)}{2} \frac{x}{2} = (2)5$	$x = 7$	$5 \quad 5$	$x = 10$	$y + 4 = -7$	$\underline{x} = \underline{\frac{7}{5}}$		$y + 4 - 4 = -7 - 4$			$y = -11$		
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Unit 3: Geometric Applications of Exponents

Volume of a Cylinder:
 $V = Bh$ $V = \pi r^2 h$
 (B = area of base: πr^2)
 (h = height of the figure)

A Coke can is 5 inches tall and has a radius of 2 inches. What is the volume of the can?

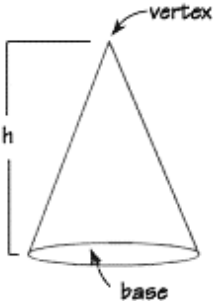
L: $r = 2$ $h = 5$
W: $V = \pi r^2 h$
P: $V = (3.14)(2^2)(5)$
C: $V = 62.8 \text{ in}^3$



Volume of a Cone:
 $V = \frac{Bh}{3}$ $V = \frac{\pi r^2 h}{3}$
 (B = area of base: πr^2)
 ($\pi \approx 3.14$)
 (r = radius)
 (h = height of the figure)

What is the volume of an ice cream cone with a radius of 3 and height of 4?

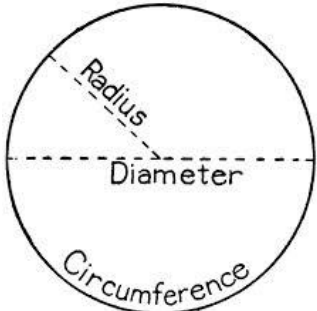
L: $r = 3$ $h = 4$
W: $V = \frac{\pi r^2 h}{3}$
P: $V = \frac{(3.14)(3^2)(4)}{3}$
C: $V = 37.7 \text{ units}^3$



Volume of a Sphere:
 $V = \frac{4\pi r^3}{3}$
 ($\pi \approx 3.14$)
 (r = radius)

You are playing softball with friends. The ball has a diameter of 10 cm. What is the volume of the softball?

L: $d = 10$ $r = 5$
W: $V = \frac{4\pi r^3}{3}$
P: $V = \frac{(4)(3.14)(5^3)}{3}$
C: $V = 523.3 \text{ cm}^3$



Label the information
 Write the formula
 Plug in the information
 Chug out the answer

The **diameter** of a circle is longest distance across a circle. (The diameter cuts through the center of the circle. This is what makes it the longest distance.)

The **radius** of a circle is the distance from the center of the circle to the outside edge.

Pythagorean Theorem:
 *only works with right triangles
 (right triangles have only 1 right angle)

$a^2 + b^2 = c^2$
a & b are legs
c is hypotenuse, longest side, opposite right angle

The Pythagorean theorem: The sum of the areas of the two squares on the legs (a and b) equals the area of the square on the hypotenuse (c).

To find the missing leg: Take the area of the hypotenuse (area of the square on the hypotenuse) – the leg squares (area of the square on the leg) = the leg squared (area of the square on the leg).

To find the length of the leg: take the square root of the area of the square on the leg.

To find the missing hypotenuse: take the leg squared (area of the square on the leg) + the leg squared (area of the square on the leg) = the hypotenuse squared (area of the square on the hypotenuse).

To find the length of the hypotenuse: take the square root of the area of the square on the hypotenuse.

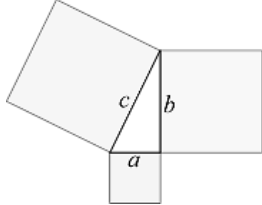
You are creating a picture frame in the shape of a right triangle. You have calculated the longest side to be 15 inches. What would be the length of the other two sides?

$a^2 + b^2 = 15^2$
 $a^2 + b^2 = 225$
 $9^2 + 12^2 = 225$
 $81 + 144 = 225$

The other two sides are 9 in. and 12 in.

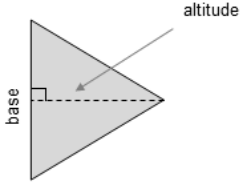
Is it a Right Triangle?
 Plug into $a^2 + b^2 = c^2$ (c is biggest #)

4, 6, 8	3, 4, 5
$4^2 + 6^2 = 8^2$	$3^2 + 4^2 = 5^2$
$16 + 36 = 64$	$9 + 16 = 25$
$52 \neq 64$	$25 = 25$
NO	YES



The Altitude of a triangle

In the case of a triangle, a common way to calculate its area is 'half base times height' where the 'height' is the altitude, or the perpendicular distance from the base to the opposite vertex. The base can be any side, not just the one drawn at the bottom.



To calculate the area you pick one side to be the base, and then measure the altitude at right angles to it.

Converse of Pythagorean Theorem:
 If the square of the length of the longest side of a triangle is equal to the sum of the squares of the lengths of the other two sides, then the triangle is a right triangle.

Length of leg/hypotenuse measured in: ft, cm, m, etc.

Area of square on leg/hypotenuse measured in: ft², cm², m², etc.

Literal Equations

Equations with multiple variables where you are asked to solve for just one of the variables.

Example:

Solve $V = \pi r^2 h$ for r .

Step 1: Divide both sides by π and h

$$\frac{V}{\pi h} = r^2$$

Step 2: Take the square root of both side to get r by itself

$$\sqrt{\frac{V}{\pi h}} = \sqrt{r^2}$$

Step 3: Solve for r .

$$\sqrt{\frac{V}{\pi h}} = r$$

Example:

Solve $V = \pi r^2 h$ for h .

Step 1: To solve for h , you will need to divide both sides by π and r^2 .

$$\frac{V}{\pi r^2} = h$$

Example:

The formula for finding the perimeter of a rectangle is

$$P = 2b + 2h. \text{ Solve for } h.$$

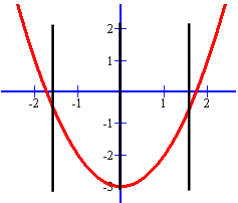
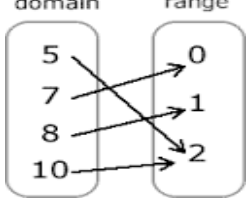
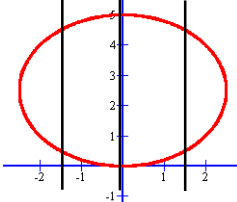
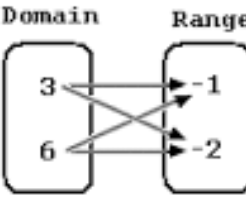
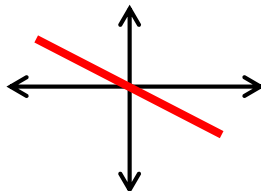
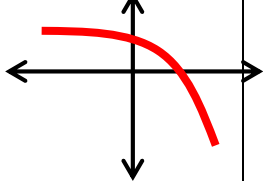
Step 1: subtract $2b$ from each side

$$P - 2b = 2h$$


Step 2: Divide both sides by 2

$$\frac{P - 2b}{2} = h$$

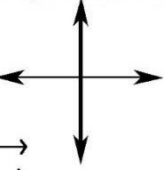
Unit 4: Functions

Function – one output for every input (x values can't repeat, pass vertical line test)		domain range 	<table border="1" style="border-collapse: collapse;"> <thead> <tr> <th style="padding: 2px 5px;">x</th> <th style="padding: 2px 5px;">y</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">8</td></tr> <tr><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">9</td></tr> <tr><td style="padding: 2px 5px;">5</td><td style="padding: 2px 5px;">10</td></tr> <tr><td style="padding: 2px 5px;">4</td><td style="padding: 2px 5px;">11</td></tr> </tbody> </table>	x	y	2	8	3	9	5	10	4	11
x	y												
2	8												
3	9												
5	10												
4	11												
Not a Function – Doesn't pass vertical line test, x values repeat...		Domain Range 	<table border="1" style="border-collapse: collapse;"> <thead> <tr> <th style="padding: 2px 5px;">x</th> <th style="padding: 2px 5px;">y</th> </tr> </thead> <tbody> <tr><td style="padding: 2px 5px;">1</td><td style="padding: 2px 5px;">3</td></tr> <tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">2</td></tr> <tr><td style="padding: 2px 5px;">2</td><td style="padding: 2px 5px;">10</td></tr> <tr><td style="padding: 2px 5px;">3</td><td style="padding: 2px 5px;">4</td></tr> </tbody> </table>	x	y	1	3	2	2	2	10	3	4
x	y												
1	3												
2	2												
2	10												
3	4												
Linear – Have to have a common difference, have the slope intercept form ($y=mx+b$), and form a straight line when graphed.	<table border="1" style="border-collapse: collapse;"> <thead> <tr> <th style="padding: 2px 5px;">x</th> <th style="padding: 2px 5px;">1</th> <th style="padding: 2px 5px;">2</th> <th style="padding: 2px 5px;">3</th> <th style="padding: 2px 5px;">4</th> </tr> </thead> <tbody> <tr> <th style="padding: 2px 5px;">y</th> <td style="padding: 2px 5px;">3</td> <td style="padding: 2px 5px;">6</td> <td style="padding: 2px 5px;">9</td> <td style="padding: 2px 5px;">12</td> </tr> </tbody> </table>	x	1	2	3	4	y	3	6	9	12		$y = 2x + 1$ $y = -9x - 4$
x	1	2	3	4									
y	3	6	9	12									
Nonlinear – Are a curved or broken line when graphed; in the equation there are exponents, variables multiplied together, or variables in the denominator.	<table border="1" style="border-collapse: collapse;"> <thead> <tr> <th style="padding: 2px 5px;">x</th> <th style="padding: 2px 5px;">5</th> <th style="padding: 2px 5px;">6</th> <th style="padding: 2px 5px;">7</th> <th style="padding: 2px 5px;">8</th> </tr> </thead> <tbody> <tr> <th style="padding: 2px 5px;">y</th> <td style="padding: 2px 5px;">2</td> <td style="padding: 2px 5px;">4</td> <td style="padding: 2px 5px;">7</td> <td style="padding: 2px 5px;">8</td> </tr> </tbody> </table>	x	5	6	7	8	y	2	4	7	8		$y = x^3$ $8 = 6xy$ $3 = \frac{3x}{y}$
x	5	6	7	8									
y	2	4	7	8									

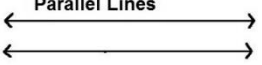
Intersecting Lines

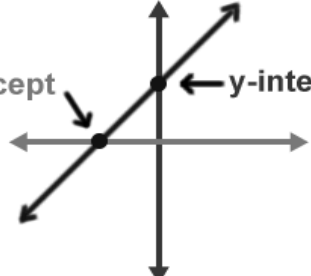


Perpendicular Lines



Parallel Lines



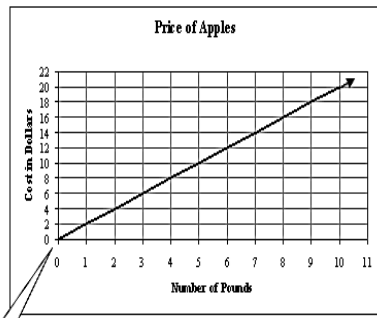


x-intercept y-intercept

Proportional Relationships

Apples for Sale
\$2.00 per pound

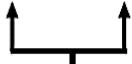
Graph



Price of Apples

Table

Price of Apples	
Number of Pounds of Apples (x)	Cost (y)
0	0
1	\$2.00
2	\$4.00
3	\$6.00
4	\$8.00
5	\$10.00



In this example, to find the cost, the number of pounds is always multiplied by \$2.00 which is the constant rate of change (k).

Unit 5: Linear Functions

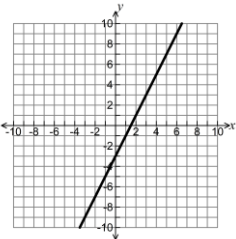
To find an equation, you always need a slope (m) and y-intercept (b)!!!!

Equation From a Graph

1. Find the y-intercept (**b**)
2. Locate another point
3. From the "b" use rise over run to get to the next point – this is your slope (**m**)
4. Put "m" and "b" into

$$y = mx + b$$

$$y = 2x - 3$$



Equation From a Table

1. Find $\frac{\text{change in } y}{\text{change in } x} = m$
2. Pick a point (x,y) and plug into $y=mx+b$ along with **m**
3. Solve for "b"
4. Put "m" and "b" into

$$y = mx + b$$

x	y
-1	-2
0	2
1	6

Difference in x is →

← Difference in y is +4

If x is 0, then this is your y-intercept

$$m = \frac{4}{1}$$

$$b = (0, 2) = 2$$

$$y = 4x + 2$$

Equation From (x_1, y_1) (x_2, y_2)

1. Find $\frac{y_2 - y_1}{x_2 - x_1} = m$
2. Pick a point (x,y) and plug into $y = mx + b$ along with **m**
3. Solve for "b"
4. Put "m" and "b" into

$$y = mx + b$$

Determine equation from points (0, -4) and (0, 5).

$$\frac{5 - (-4)}{0 - 0} = \frac{5 + 4}{0} = \frac{9}{0} = \text{undefined slope}$$

(remember equation is $x =$)

$$x = 0$$

Standard Form

$$ax + by = c$$

Convert to slope intercept form

move ax to opposite side with opposite sign ($by = -ax + c$)

1. y stands alone; divide everything by b

$$\left(y = \frac{a}{b}x + \frac{c}{b}\right)$$

2. y cannot be negative (change everything in equation to opposite sign (multiplying by -1))

Word Problem

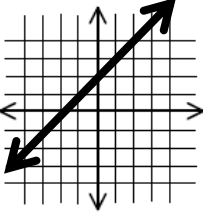
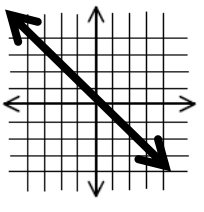
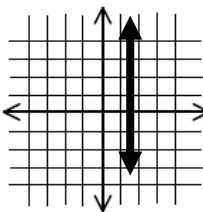
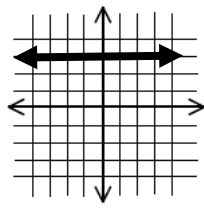
The distance traveled on a trip is directly proportional to the speed of the car. A car traveled 300 miles in six hours. Write an equation to represent y, the distance the car would travel in x hours.

REMEMBER: Unit Rate = SLOPE

$$\frac{300}{6} = 50$$

$$y = 50x$$

Types of SLOPE

POSITIVE SLOPE	NEGATIVE SLOPE	UNDEFINED SLOPE	ZERO SLOPE
Graphed line moves upward from left to right.	Graphed line moves downward from left to right.	Graphed line is a vertical line (straight up and down).	Graphed line is a horizontal line .
Example: 	Example: 	Example: 	Example: 
Example: $y = 6x + 1$ $y = \frac{2}{3}x - 4$	Example: $y = -3x + 2$ $y = -\frac{2}{5}x - 1$	Example: $x = 4$ $x = -6$ $x = 3$	Example: $y = 5$ $y = -2$ $y = 8$

Unit 6: Linear Models & Tables

Rate of Change

Increasing – positive slope	Decreasing – negative slope	Greatest ROC= Ignore the sign (doesn't matter if positive or negative) and choose biggest number	Least ROC = Ignore the sign (doesn't matter if positive or negative) and choose smallest number
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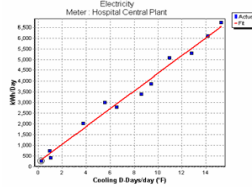
Stories from Graphs

Going away from = distance increasing = positive slope	Going towards = distance decreasing = negative slope	Running = steeper line	Walking = less steep line
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Line of Best Fit

1. Put your ruler in the middle of as many points as possible

2. Draw a straight line across whole graph (This line may pass through some of the points, none of the points, or all of the points).

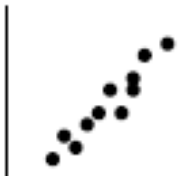


3. Find your "b" - Look at where the line crosses the y-axis

4. Find your slope = pick two points and count rise over run.

Scatter Plots

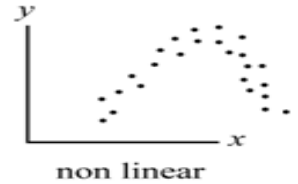
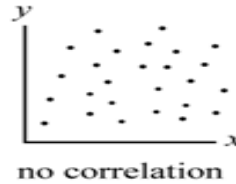
Strong Correlation – close together
Weak Correlation – far apart



Strong Positive Correlation



Weak Positive Correlation

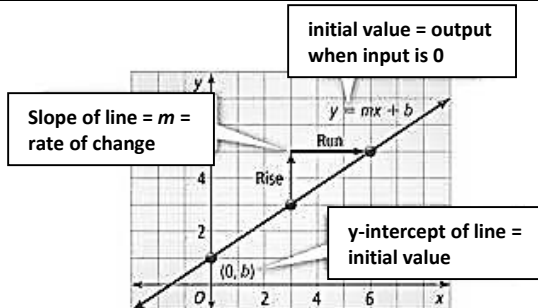


Strong Negative Correlation



Weak Negative Correlation

Initial Value and Rate of Change



Joint and Marginal Frequencies

	Spanish	French	German	Total
Boys	10	2	8	20
Girls	15	12	3	30
Total	25	14	11	50

Joint Frequencies (points to the inner table)

Marginal Frequencies (points to the outer rows and columns)

Two-Way Tables and Relative Frequency Tables

Two-Way Frequency Table

	Spanish	French	German	Total
Boys	10	2	8	20
Girls	15	12	3	30
Total	25	14	11	50

\longrightarrow
 Divide all table entries
 by the table total (50)
 \longrightarrow

Two-Way Relative Frequency Table
 (with respect to table total)

	Spanish	French	German	Total
Boys	0.2	.04	0.16	0.40
Girls	0.3	0.24	0.06	0.60
Total	0.5	0.28	0.22	1.00

Variables

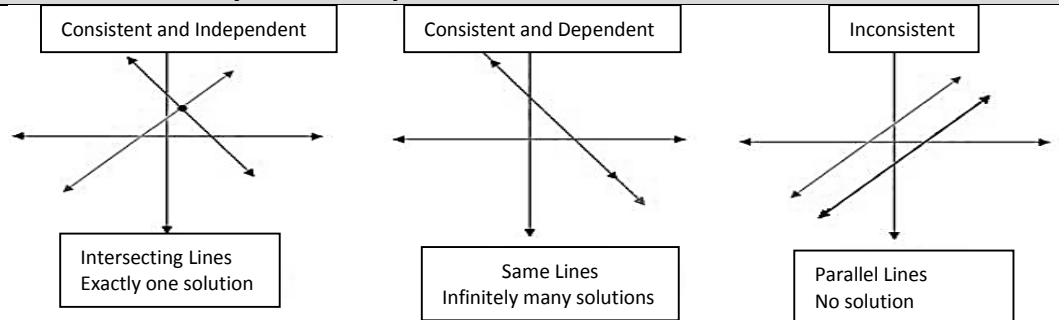
Variables can be classified as **categorical** (aka, qualitative) or **quantitative** (aka, numerical).

- Categorical. Categorical variables take on values that are names or labels. The color of a ball (e.g., red, green, blue) or the breed of a dog (e.g., collie, shepherd, terrier) would be examples of categorical variables.
- Quantitative. Quantitative variables are numerical. They represent a measurable quantity. For example, when we speak of the population of a city, we are talking about the number of people in the city - a measurable attribute of the city. Therefore, population would be a quantitative variable
- An outlier is an observation that lies outside the overall pattern of a distribution. Usually, the presence of an outlier indicates some sort of problem. This can be a case which does not fit the model under study, or an error in measurement.

Unit 7: Systems of Equations

Solution: (x,y)

Where the lines intersect



3 Methods to Solving Systems:

GRAPHING

- Both equations must be written as $y = mx + b!$
- Graph both the lines and see where they meet!

SUBSTITUTION

- Single out x or y and then plugging this back into the other equation, "substituting" for the chosen variable and solving for the other.
- Then you back-solve for the first variable.

ELIMINATION

- Line them up.
- Look for matching coefficients.
- Add/subtract to eliminate.

Elimination

$$\begin{cases} 3y + 2x = 6 \\ 5y - 2x = 10 \end{cases}$$

Eliminate the x-variable by addition of the two equations.

$$\begin{array}{r} 3y + 2x = 6 \\ + 5y - 2x = 10 \\ \hline 8y = 16 \\ y = 2 \end{array}$$

The value of y can now be substituted into either of the original equations to find the value of x.

$$\begin{array}{r} 3y + 2x = 6 \\ 3(2) + 2x = 6 \\ 6 + 2x = 6 \end{array}$$

Substitution

$$y = x + 1 \quad 2y = 3x$$

$$2y = 3x$$

$$2(x + 1) = 3x$$

$$\begin{array}{r} 2x + 2 = 3x \\ -2x \quad -2x \\ \hline 2 = x \end{array}$$

$$2 = x$$

$$y = x + 1$$

$$y = 2 + 1 = 3$$

Solution: (1, 3)

Graphing

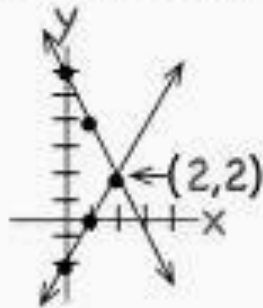
Find the Solution

$$2x - y = 2$$

$$y = 2x - 2$$

$$2x + y = 6$$

$$y = -2x + 6$$



Solution: (2, 2)

$$2x - y = 2$$

$$2(2) - 2 \stackrel{?}{=} 2$$

$$4 - 2 \stackrel{?}{=} 2$$

$$\checkmark 2 = 2$$